Logical Foundations of Secure Resource Management in Protocol Implementations

 ${\sf Matteo~Maffei}^1 \\ {\sf joint~work~with~Michele~Bugliesi}^2, {\sf Fabienne~Eigner}^1 {\sf ~and~Stefano~Calzavara}^2 \\$

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POST'13, best EATCS paper award at ETAPS'13.

Outline

- Why? (Beyond FOL refinements)
- What? (Affine logic for security protocols)
- How? (Proof techniques)

Verified implementations

- narrow the gap between formal model and implementation
- combine type-checking with general-purpose theorem proving
- efficient and modular verification

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 - assertions: formulas which must be entailed by the assumptions

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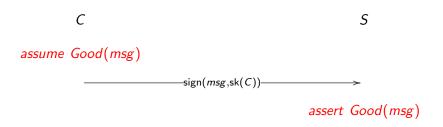
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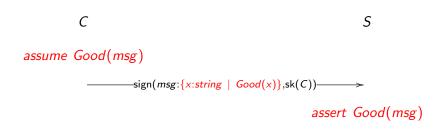
Methodology

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 - assumptions: formulas which are assumed to hold
 - assertions: formulas which must be entailed by the assumptions
- type-check the code against appropriate refinement types
- well-typed programs are robustly safe: assertions are always entailed by the introduced assumptions, even in presence of an opponent

A glance at refinement typing



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A glance at refinement typing

$$C \hspace{1cm} S$$

$$assume \hspace{0.1cm} Good(msg)$$

$$-----sign(msg:\{x:string \mid Good(x)\},sk(C)) \longrightarrow$$

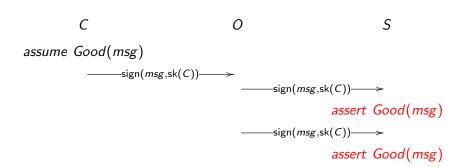
$$assert \hspace{0.1cm} Good(msg)$$

Refinement typing

```
sk(C): SigKey({x : string | Good(x)})
```

- C must prove that Good(msg) holds true upon signing
- S can rely on Good(msg) being true upon verification

Replays



This run is safe...

In FOL: $Good(msg) \vdash Good(msg) \land Good(msg)$

...but sometimes it should not!

• What if Good(msg) expresses a bank transaction?

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Resource-aware properties

Counting

Some properties require to count the number of times a certain resource is used (or an action is performed)

- Injective agreement or strong authentication: every end-event is preceded by a distinct begin-event
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Affine (or resource-aware) logic

Such properties can be naturally expressed in affine logic (no contraction)

- affine hypotheses A can be used at most once
- exponential hypotheses !A can be used arbitrarily often

For instance, $Good(msg) \not\vdash Good(msg) \otimes Good(msg)$ (\otimes denotes conjunction in affine logic)

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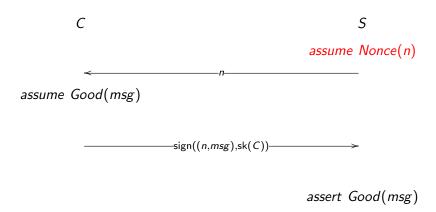
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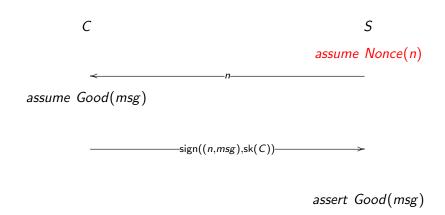
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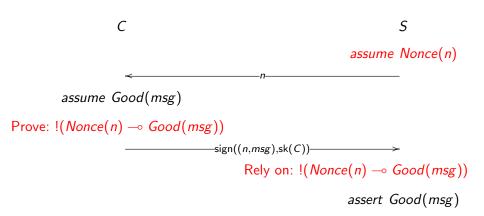
(⊗ denotes conjunction in affine logic)

How can we type-check cryptographic protocols that achieve resource-aware properties?

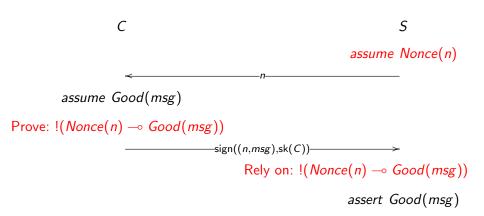




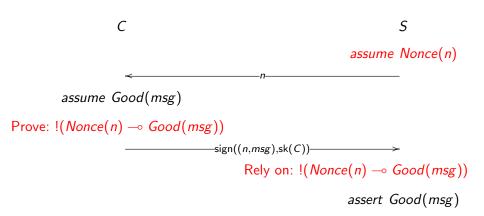
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Guarded refinement types sk(C) : SigKey(x : int, \{y : string \mid !(Nonce(x) \multimap Good(y))\})
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```
Type-checking the assertion
Nonce(n), !(Nonce(n) \multimap Good(msg)) \vdash Good(msg)
```



Preventing duplication

Nonce(n), $!(Nonce(n) \multimap Good(msg)) \nvdash Good(msg) \otimes Good(msg)$

Contributions

- a theory of exponential serialization
- a type system for enforcing affine logic policies on application code

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 - even in presence of an arbitrary opponent

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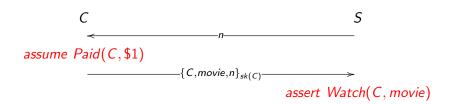
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Example: a streaming service

Authorization policy

$$\mathcal{P} = ! \forall x, y. (Paid(x, \$1) \multimap Watch(x, y))$$

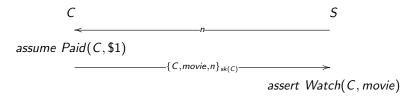
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Implementing the streaming service



Implementing the streaming service

```
assume Paid(C, \$1)
                       ---\{C, movie, n\}_{sk(C)}
                                           assert Watch(C, movie)
let client C addC addS m sk =
    let xn = recv addC in assume Paid(C,$1);
    let msg = sign (C,m,xn) sk in send addS msg
val mkNonce: unit -> {x: bytes | Nonce(x)}
let serv S addC addS vk =
    let n = mkNonce () in send addC n;
    let msg = recv addS in
    let (xC, xm, xn) = verify msg vk in
    if (xn = n) then
        assert Watch(xC,xm)
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Type-checking the server

Verification key type

 $vk : VerKey(x : T_c, y : T_m, \{z : T_n \mid !(Nonce(z) \multimap Paid(x, \$1))\})$

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Type-checking the assertion

if (xn = n) then

Recall $\mathcal{P} = ! \forall x, y. (Paid(x, \$1) \multimap Watch(x, y))$, we have:

// !(Nonce(xn) --o Paid(xC,\$1)) holds true

// !(xn = n) holds true
assert Watch(xC,xm)

 \mathcal{P} , Nonce(n), !(xn = n), $!(Nonce(xn) \multimap Paid(xC, \$1)) \vdash Watch(xC, xm)$

Type-checking the client

Signing key type

 $\mathit{sk} : \mathit{SigKey}(x : T_c, y : T_m, \{z : T_n \mid !(\mathit{Nonce}(z) \multimap \mathit{Paid}(x, \$1))\})$

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- This implies that the signing operation is not well-typed!

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Solution

Add an explicit serializer among the assumptions

$$S = ! \forall x, y. (Paid(x, \$1) \multimap ! (Nonce(y) \multimap Paid(x, \$1)))$$

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Notice that we have:

$$S$$
, $Paid(C, \$1) \vdash !(Nonce(xn) \multimap Paid(C, \$1))$

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In the paper we identify sufficient syntactic conditions for soundness

Overview of the type system

Typing environments

Type judgements of the form Γ ; $\Delta \vdash \mathcal{J}$

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Typing rules

General structure of a typing rule

$$\frac{\Gamma; \Delta_1 \vdash \mathcal{J}_1 \qquad \dots \qquad \Gamma; \Delta_n \vdash \mathcal{J}_n \qquad \Delta \hookrightarrow \Delta_1, \dots, \Delta_n}{\Gamma; \Delta \vdash \mathcal{J}}$$

The rewriting $\Delta \hookrightarrow \Delta'$ allows for manipulating the logical context according to the entailment relation (e.g., split conjunctions or duplicate exponential resources)

Example

Standard Refinement Typing

VAL REFINE
$$\frac{\Gamma; \Delta \vdash M : T \qquad \Gamma; \Delta \vdash F\{M/x\}}{\Gamma; \Delta \vdash M : \{x : T \mid F\}}$$

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We have to choose where to use affine resources:

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E.g.,
$$M:T$$
; $A \otimes B \vdash M: \{y: \{x:T \mid A\} \mid B\}$ since $A \otimes B \hookrightarrow A, B$

Environment rewriting is highly non-deterministic and this hinders the implementation of a type-checker:

- the type-checker should incorporate logical entailment...
- ... and distribute formulas among subderivations

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- algorithmic type-checking is sound and complete

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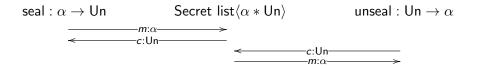
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Affine Refinement Typing

- Values are partially annotated to make type-checking syntax-directed
- The algorithmic typing rules collect the formulas required for typing, which are then automatically discharged:

VAL REFINE
$$\frac{\Gamma \vdash_{\mathsf{alg}} M : T; F'}{\Gamma \vdash_{\mathsf{alg}} M_{\{x: \bot F\}} : \{x : T \mid F\}; F' \otimes F\{M/x\}}$$

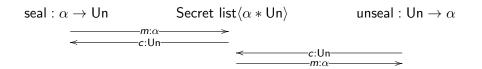
Typing cryptographic libraries



Symbolic cryptography

We prove properties in the symbolic setting, using standard *sealing-based* cryptographic libraries developed for F7/F*

Typing cryptographic libraries



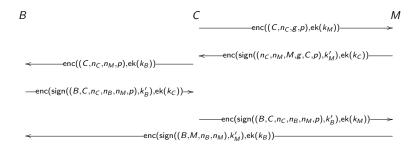
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Key aspects

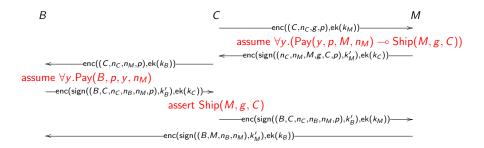
- Communication and cryptographic libraries build on *exponential types*, which do not carry any affine refinements (they are all serialized)
- Consequently, we can just reuse standard typed cryptographic libraries

An e-commerce protocol proposed by Guttman et al.¹



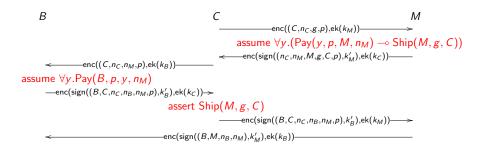
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Verification

- we enrich the code with suitable (refinement) types
- 2 we introduce the necessary serializers
- we type-check the protocol

The proof obligation is dispatched by 11prover in less than 20 ms (nevertheless, automated theorem provers for affine logic are far from being optimal)

Affine logic for security

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- Affine security properties for distributed systems can be statically enforced, modularly and efficiently

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Under the hood...

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- We designed a modular refinement type system for enforcing resource-aware authorization policies in protocol implementations

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- We designed a modular refinement type system for enforcing resource-aware authorization policies in protocol implementations
- We devised a sound and complete algorithmic variant
- We showed the expressiveness of our framework by type-checking the implementation of
 - a variant of the EPMO protocol
 - Kerberos

Thank you for your attention!